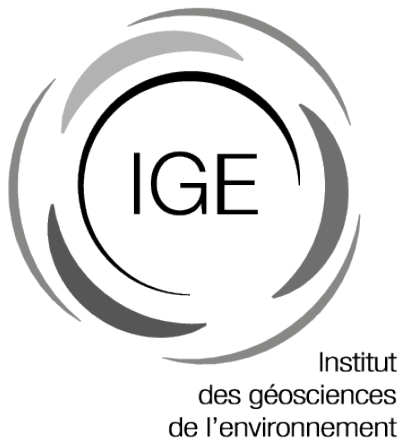


Gyre Turbulence

Interfaces dans le système climatique, 27/05/2024



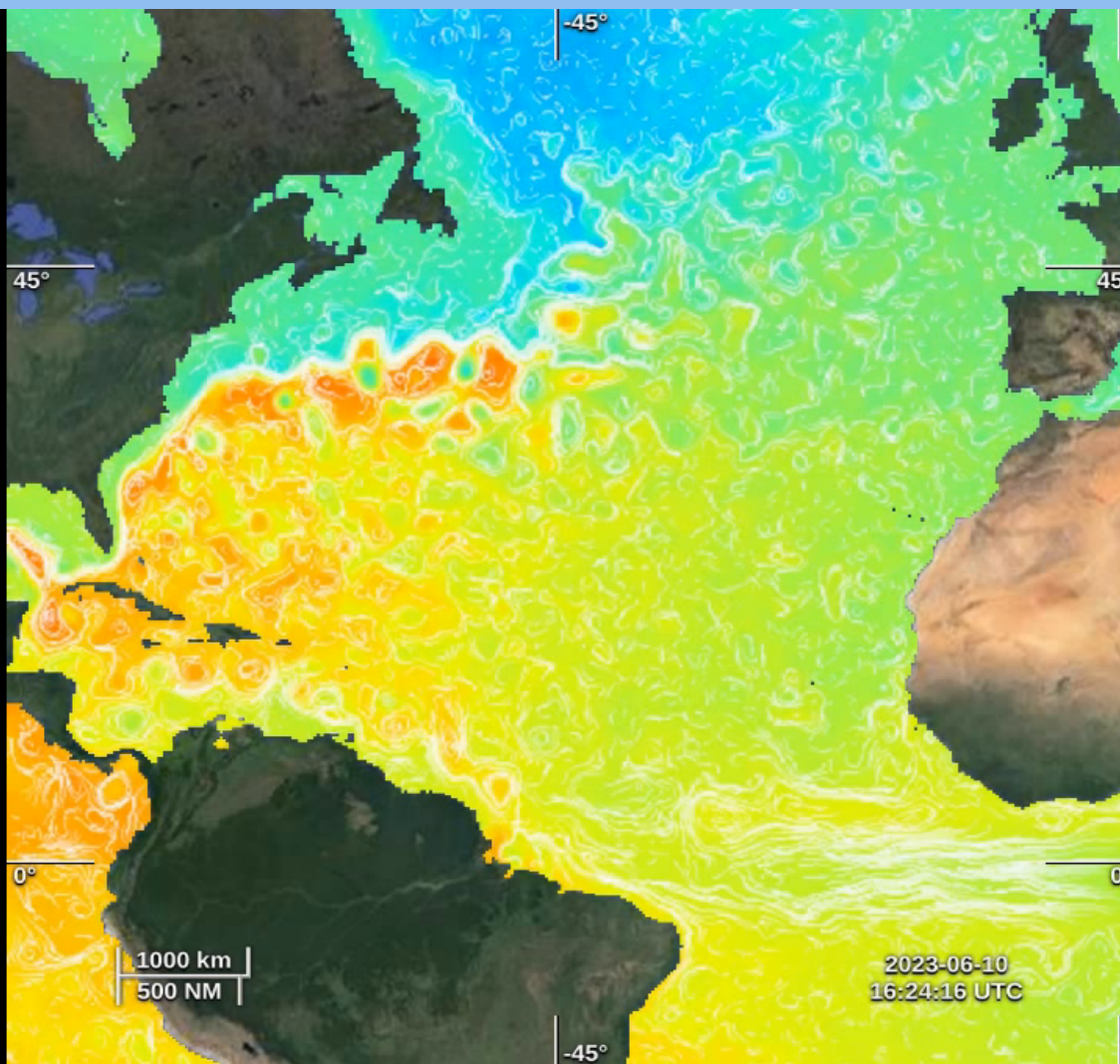
Lennard Miller

Supervisors:

Antoine Venaille (ENS de Lyon)

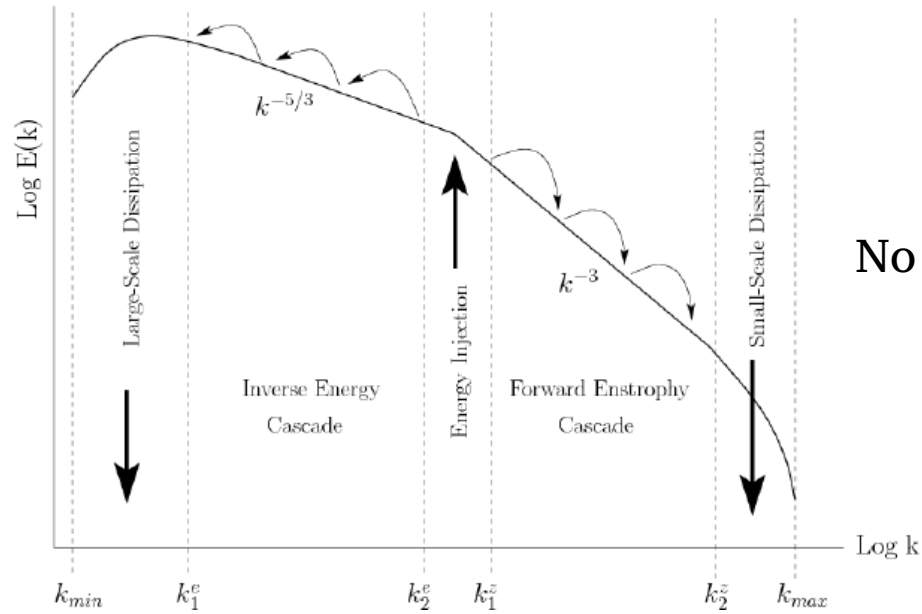
Bruno Deremble (UGA)





2D Oceanic Turbulence – Theory

Energy Transfer in **unbounded** 2D turbulence

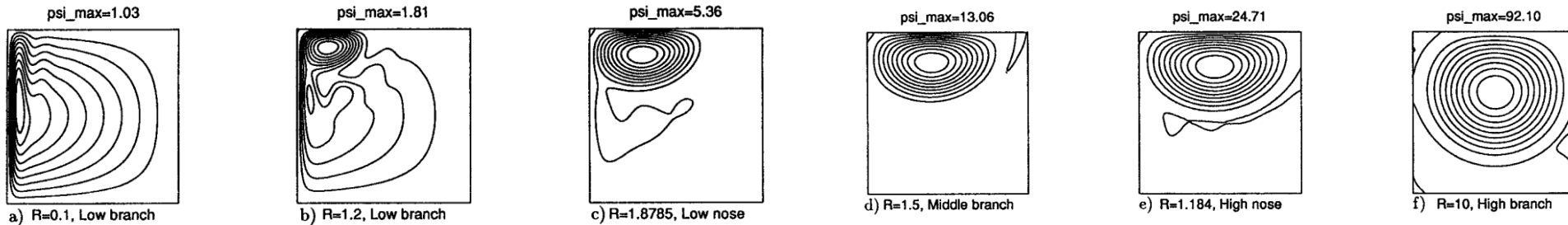


No dissipation when $\nu \rightarrow 0$

Farazmand et al. 2011

Aim of PhD: **Can coasts lead to efficient dissipation?**

Early Gyre Studies



Sverdrup Gyres
direct “ β cascade” wins

decrease ν →

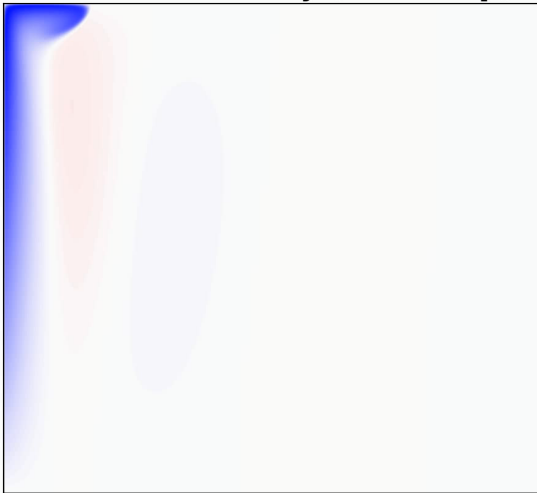
Inertial Runaway
Inverse cascade wins

“ ... the circulation does not, nor should it, saturate in the limit of vanishing lateral viscosity. ... Barotropic instability alone, we argue, is insufficient to retard the increase in recirculation beyond realistic values. ”

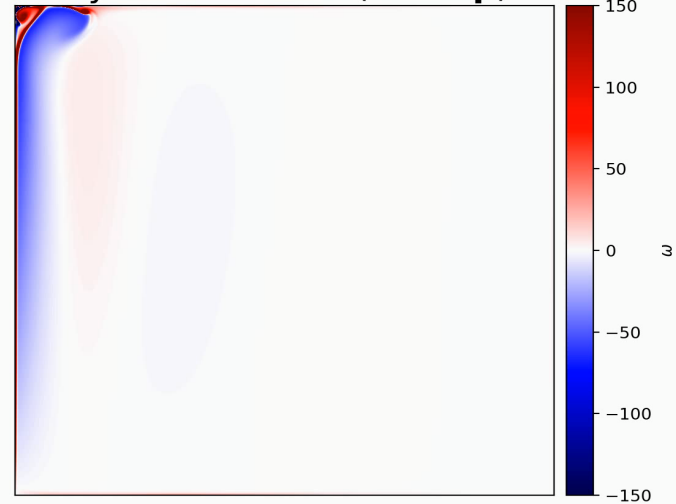
Sheremet et. al, 1997

Boundary Conditions!

Inertial Runaway (**free-slip**)



Gyre Turbulence (**no-slip**)



$$\beta^* = 100, \nu^* = 10^{-5}$$

Gyre Turbulence

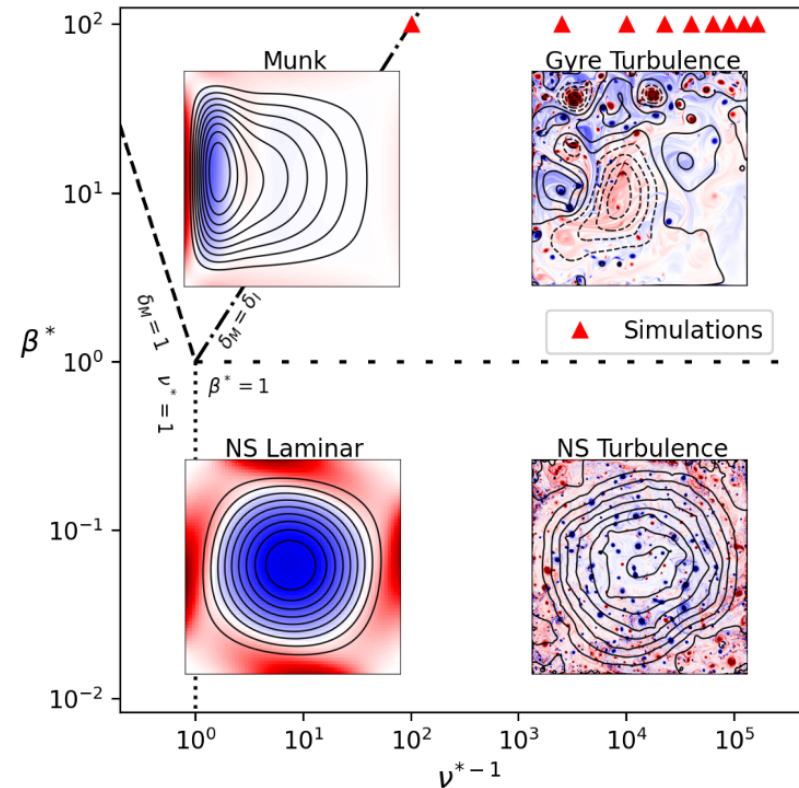
Governing Equation:

$$\frac{\partial \omega}{\partial t} + u \cdot \nabla \omega + \beta v = \nu \nabla^2 \omega - \frac{\tau}{L} \pi \sin\left(\frac{\pi y}{L}\right)$$

Non-dimensional Parameters:

$$\nu^* = \frac{\nu}{\sqrt{\tau_0} L^3}, \quad \beta^* = \beta \sqrt{\frac{L^3}{\tau_0}}$$

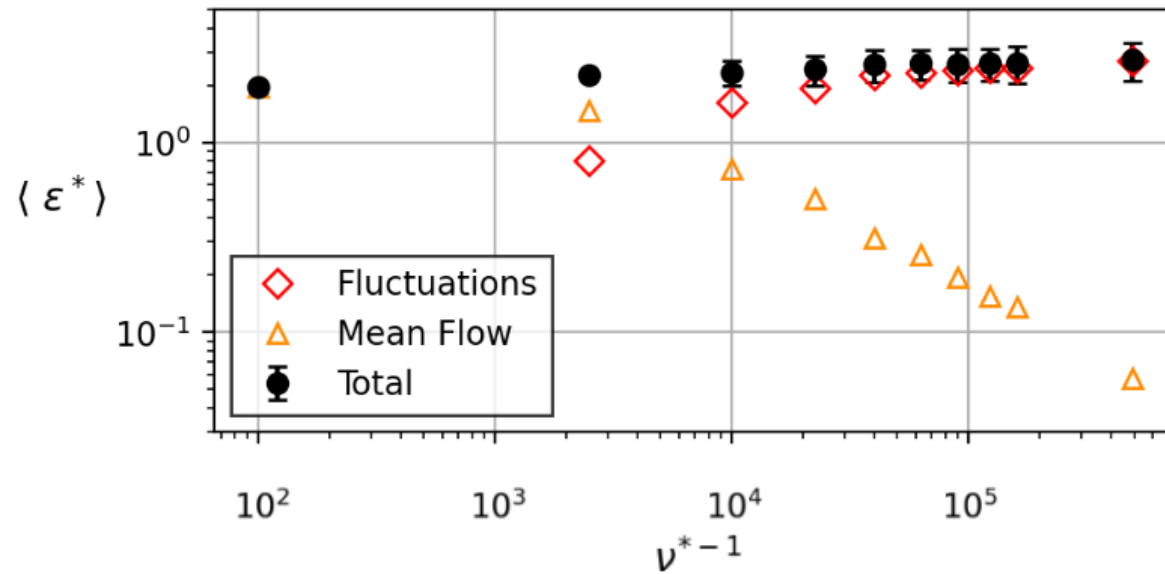
No-slip Boundary Conditions



Aim of the study: Explore limit of $\beta^* > 1$, $\nu^* \rightarrow 0$ (**Gyre Turbulence**)

A 2D finite-dissipation limit

$$\varepsilon = \nu \int \omega^2 dA = \nu \int \bar{\omega}^2 + \overline{\omega'^2} dA$$



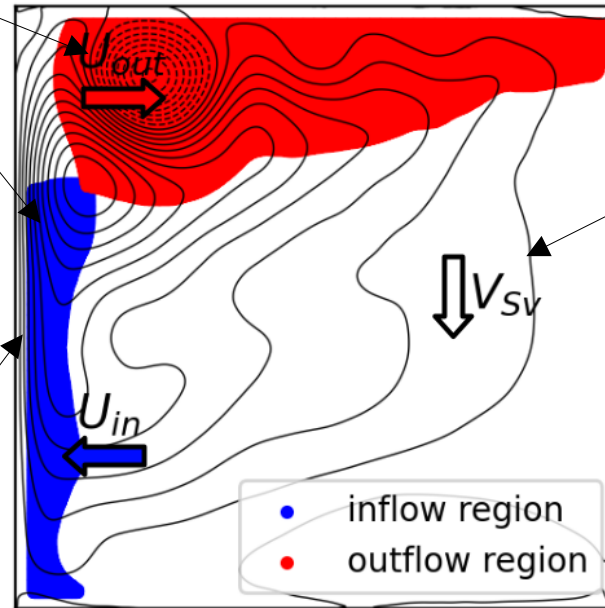
“Anomalous Dissipation”

Mean Flow

Inertial Layers

Viscous Sublayers

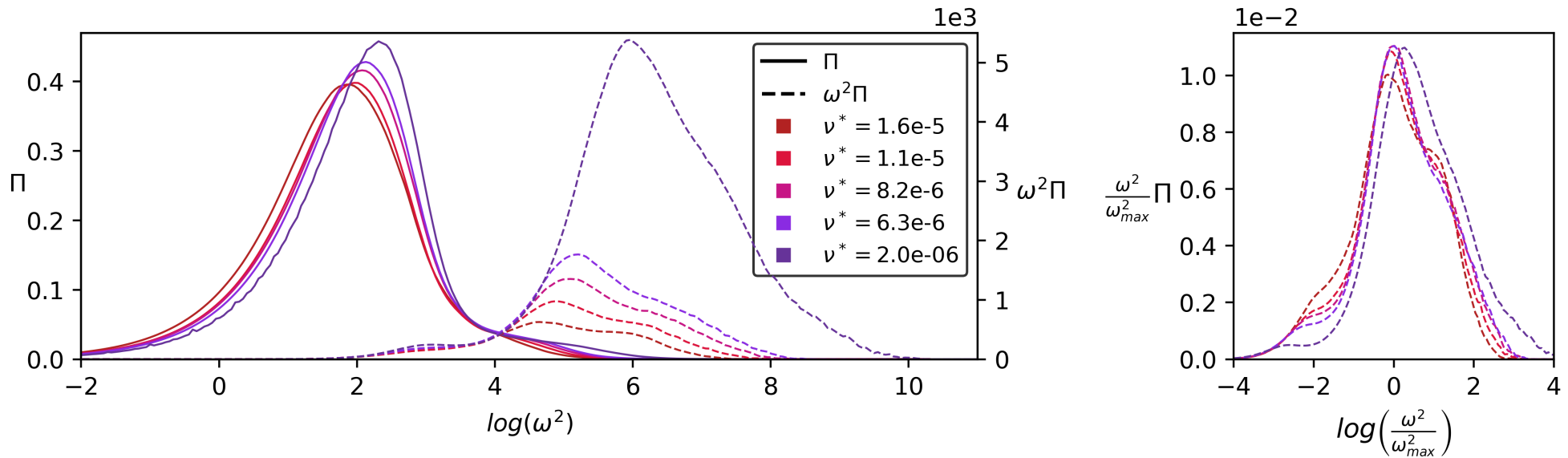
$$\omega_{max} \sim 1/\sqrt{\nu}$$



Sverdrup Flow

Vorticity Statistics

$$\varepsilon = \nu \int \omega^2 dA = \nu \int \omega^2 \Pi (\log(\omega^2)) d \log (\omega^2)$$

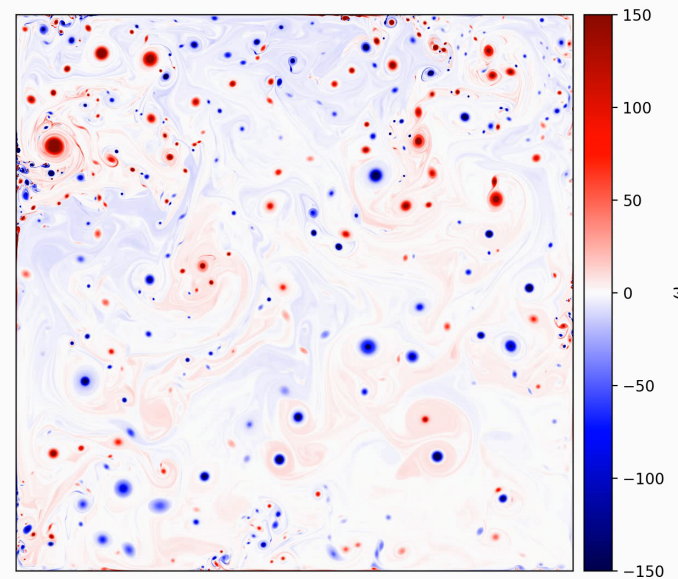


Collapse onto unity
 $\rightarrow \omega_{max}$ sets vortex maxima

Summary

- **Gyre Turbulence** is an inviscid regime with **finite dissipation rate**
- **No-slip** boundary conditions and **strong β -effect** are critical
- A barotropic model can contain a **finite inviscid energy cycle**

Gyre Turbulence (Vortex Gas Regime)



$$\beta^* = 100, \nu^* = 2 \times 10^{-6}$$